

# THE GC SCHOOL OF CAREERS

## DEPARTMENT OF MATHEMATICS

### REVISION GUIDE

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#### CORE MATHEMATICS 4

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#### COORDINATE GEOMETRY

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#### Key Points

##### 1. Cartesian equation

To find the cartesian equation of a curve, use the parametric pair of equations and try to eliminate the parameter (usually  $t$  or  $\theta$ ).

*Method 1:* If the parametric equations are not trigonometric rearrange one of them and use the substitution method.

*Method 2:* If the parametric equations are trigonometric then choose the appropriate trigonometric formula and substitute both parametric equations there. (PRACTICE)

##### 2. Using the parametric equations to find:

- **x- intercept** ( $y = 0$ )

Substitute  $y = 0$  into the parametric equation containing  $y$  and find the value(s) of  $t$ . Substitute the value(s) of  $t$  into the parametric equation containing  $x$  to find the  $x$ -coordinate.

- **y-intercept** ( $x = 0$ )

Substitute  $x = 0$  into the parametric equation containing  $x$  and find the value(s) of  $t$ . Substitute the value(s) of  $t$  into the parametric equation containing  $y$  to find the  $y$ -coordinate.

- **Point(s) of intersection with a line**

Substitute the parametric equations into the line to create an equation containing  $t$  only. Solve to find the value(s)  $t$ . Then substitute the value(s) into both parametric equations to find the  $x$  and  $y$  coordinates of the point(s) of intersection.

##### 3. Area under the curve

- Using the Cartesian equation

$$\int_{x_1}^{x_2} (y) dx$$

- Using the parametric equations

$$\int_{t_1}^{t_2} \left( y \cdot \frac{dx}{dt} \right) dt$$